

Arsenic and old models

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- ▶ Decision analysis
- ▶ Regression models

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Natural arsenic in well water in Bangladesh

- ▶ Where is the arsenic?
- ▶ What can people do?
- ▶ Digging low-arsenic wells
- ▶ Will people switch?

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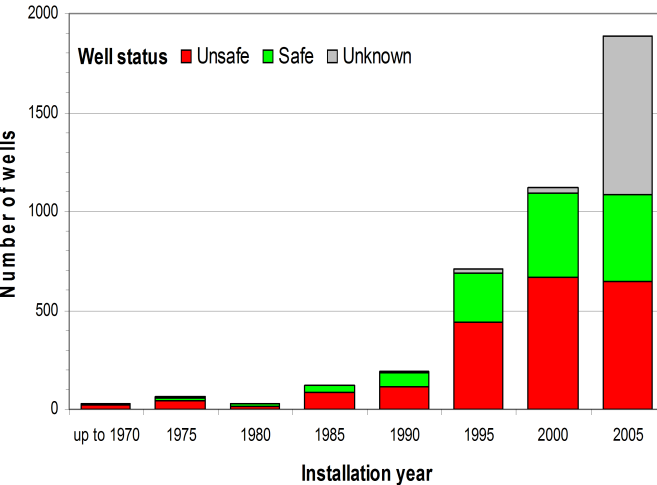
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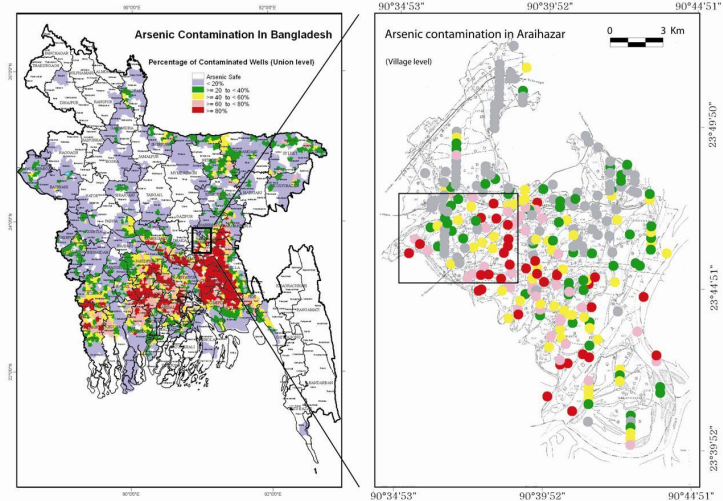
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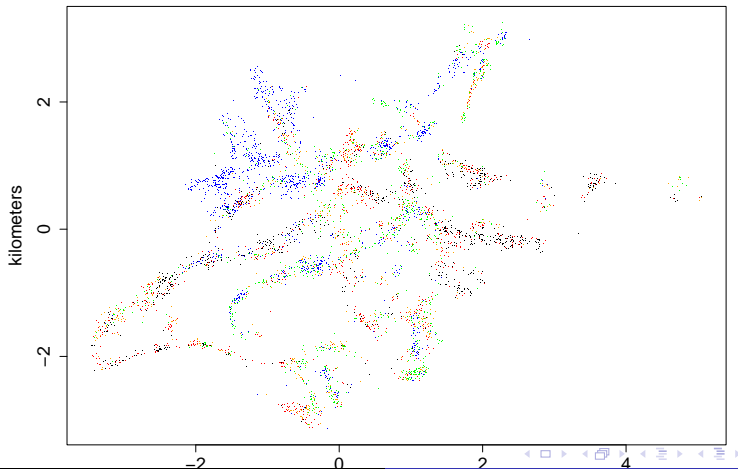
Natural arsenic in well water



Mix of high and low arsenic wells

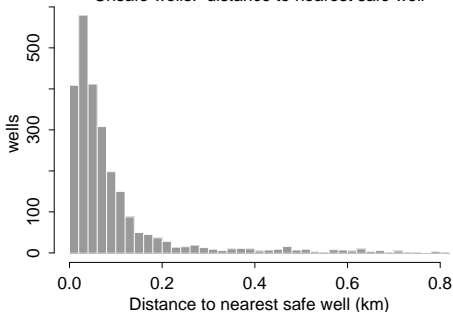


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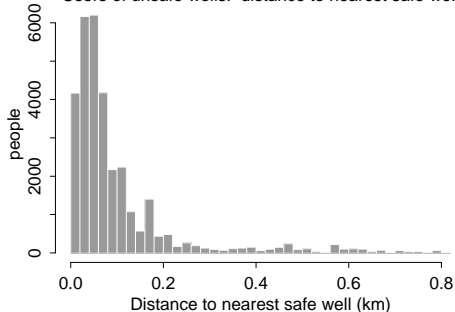


Distance to nearest safe well

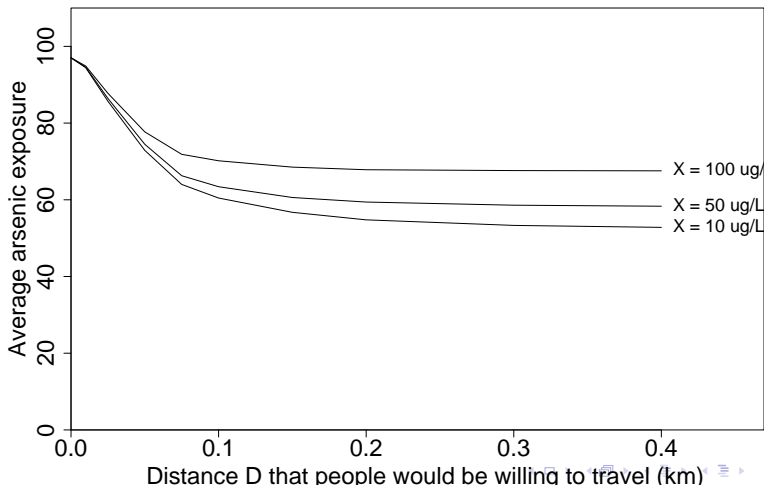
Unsafe wells: distance to nearest safe well



Users of unsafe wells: distance to nearest safe well



What if people switch wells?

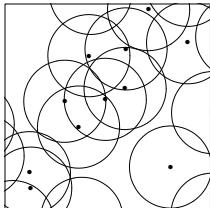
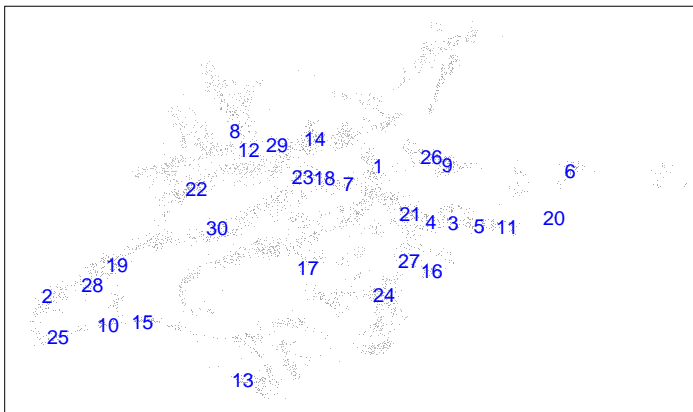


Digging new wells

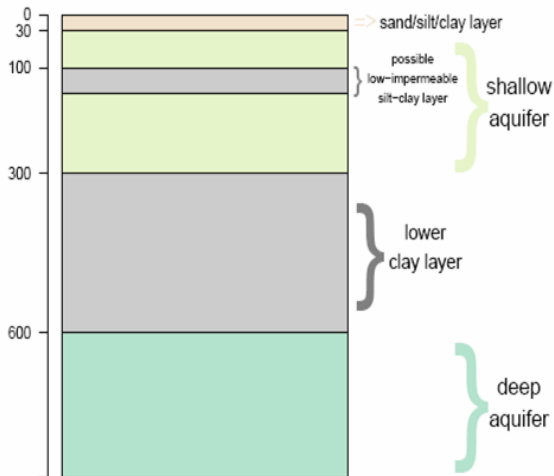
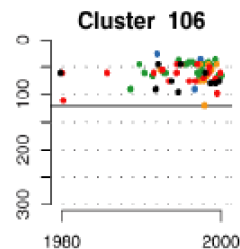
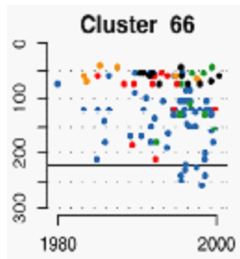


Where to dig new wells

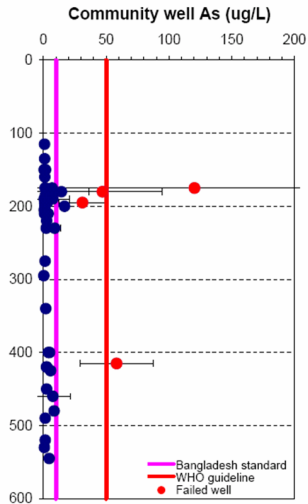
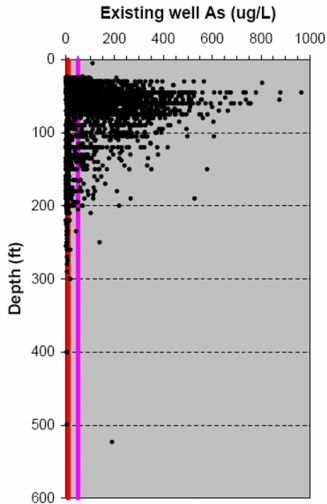
Optimal locations for 30 new safe wells
(assuming 50% of eligible people have switched already)



How deep to dig?



New community wells



Cellphone-based information system

Instructions:

SMS “?” to +880 1713 045 512
or <http://www.ideo.columbia.edu/welltracker/>

Find village?

“F*U*Araihazar*V*Bara Barai Para”

Response:

U:Araihazar
M: Bara Barai Para
Bara Barai Para, 167029410201”
and others

Safe depth?

“SD*167029410201”

Response:

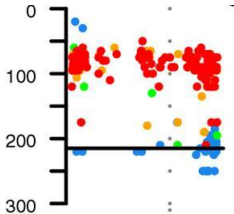
U=Araihazar
M=Bara Barai Para
V=Bara Barai Para
Start>=215’
Fail=5/100
Average arsenic 168 ppb
39 safe of 183
20-135’ 7 of 142
175-250’ 32 of 41

Money-back?

“SD*167029410201*15000”

Response:

TK750 insures TK15000 (US\$250)
Add TK1000-3000 fixed cost (well design, test)



Survey data: would you switch wells?

- ▶ Logistic regression
- ▶ Predictor variables:

Distance to nearest arsenic well

Arsenic level in your current well

Education

Number of wells in the village (not necessarily used)

Survey data: would you switch wells?

- ▶ Logistic regression
- ▶ Predictor variables:
 - ▶ Distance to nearest safe well
 - ▶ Arsenic level of your current well
 - ▶ Education
 - ▶ Membership in community arsenic committee (not profitable)

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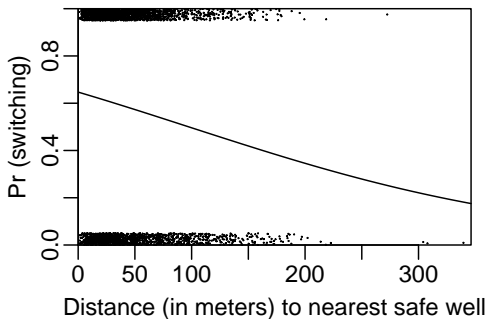
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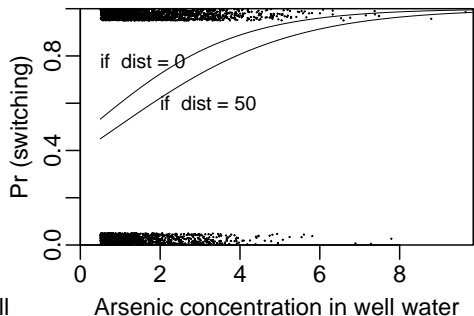
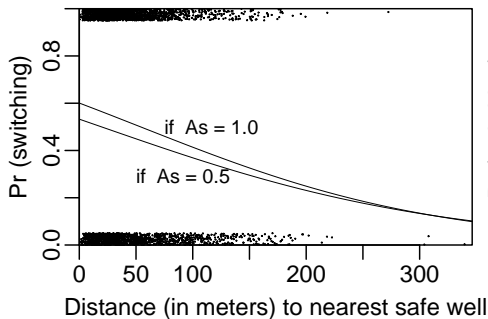
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Probability of switching wells, given distance to nearest safe well

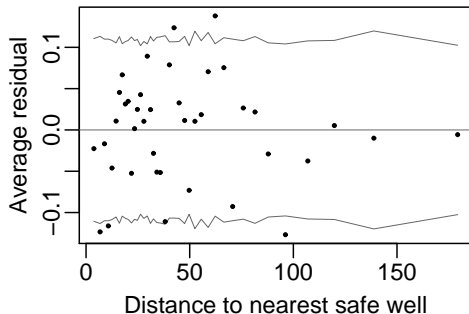


Probability of switching wells, given distance and existing arsenic level

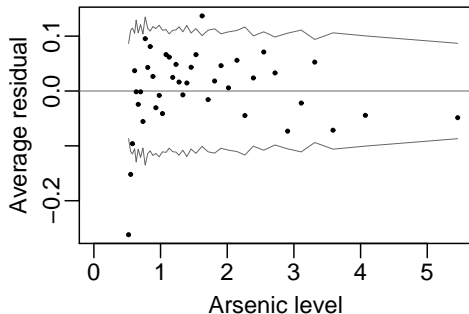


Binned residuals: are people switching more or less than predicted by the model?

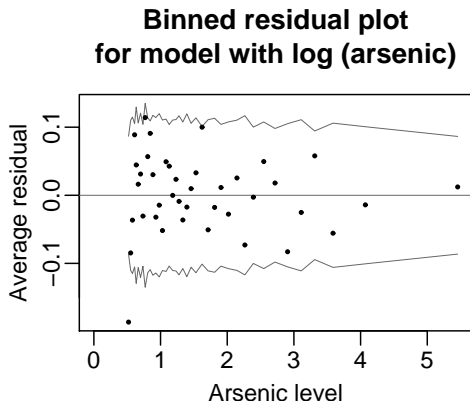
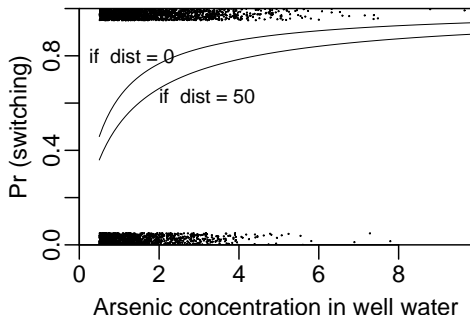
Binned residual plot



Binned residual plot



Model on log (arsenic level) and binned residuals



Model for switching

- ▶ Distance to walk comes in linearly
 - ▶ Does this make sense?
 - ▶ Yes
- ▶ Current arsenic level comes in on the log scale

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Insurance program

- ▶ Goal: dig more safe wells
- ▶ Outcomes to avoid:
 - ▶ Digging an unsafe well and not testing it
 - ▶ Not digging a safe well because afraid of wasting money on an unsafe well
 - ▶ Digging too shallow (risk of unsafe)
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- ▶ A (possible) solution: insurance or money-back guarantee

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- ▶ Arsenic example
- ▶ Institutional decision analysis and the role of centralized information collection and analysis

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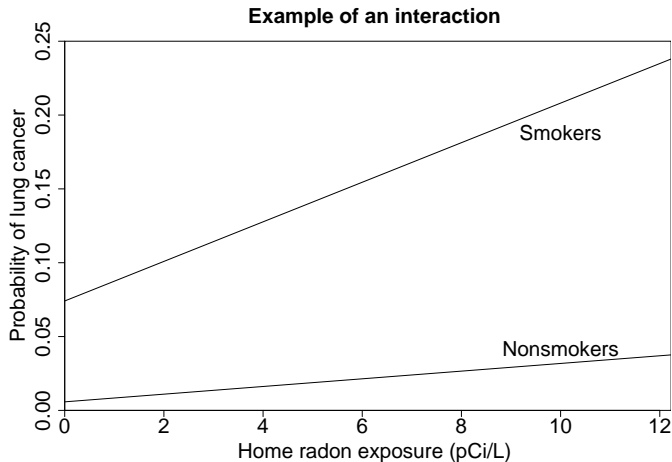
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Radon and lung cancer: estimated risks



Home radon exposure as a decision problem

- ▶ For your house, decision options:
 - ▶ Remediate (seal the basement, etc.), costs \$2000
 - ▶ Take a good measurement, costs \$50 + wait 1 year
 - ▶ Take a noisy measurement, costs \$25 + wait 1 week
 - ▶ Do nothing
- ▶ It's a classical "value of information" decision problem!

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- ▶ 3 sources of information:
 - ▶ National survey: accurate measurements in 5000 homes in 125 U.S. counties
 - ▶ State surveys: noisy, biased measurements in 80,000 homes in all the counties
 - ▶ Geophysical and geological measurements (from 1950s)
 - ▶ County-level geological maps

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Home radon analysis: statistical methods

- ▶ Classical method 1: use national survey to predict radon from house-level predictors (basement, ventilation, construction, county uranium, soil type, . . .)
- ▶ Classical method 2: use state surveys to identify high-radon areas, then link these to geological maps
- ▶ Bayesian method: combine all the info to get inference for houses with and without basements in all counties
- ▶ Measurement-error model adjusts for low-quality data
- ▶ Cross-validation demonstrates that it works

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Home radon analysis: garbage in, garbage out

- ▶ Use Bayes posterior distribution to figure out optimal decision for houses in every county
 - ▶ Average over the 3000 counties to estimate the total dollar cost and lives saved under various strategies
 - ▶ Compare to costs of other safety measures
 - ▶ Garbage-in, garbage-out issue:
- ▶ What should the EPA say?

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- ▶ Garbage-in, garbage-out issue:
 - ▶ “We found no evidence that radon levels are higher in counties with higher arsenic levels.”
 - ▶ “Specifically, we found that the mean radon level in counties with the highest arsenic levels was 1.1 pCi/L, compared to 1.0 pCi/L in counties with the lowest arsenic levels.”
 - ▶ What should the EPA say?

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Why are textbook examples of decision analysis so lame?

- ▶ Your nephew is renting an apartment, balancing issues of cost, size, convenience, . . .
- ▶ Widgets cost \$2 to make and sell for \$3. Here's the distribution of the market for widgets, . . . , how many should you make?
- ▶ Vague business example
 - ▶ Specific business example—what kind of power plant to build—pure GIGO
- ▶ Vague military example

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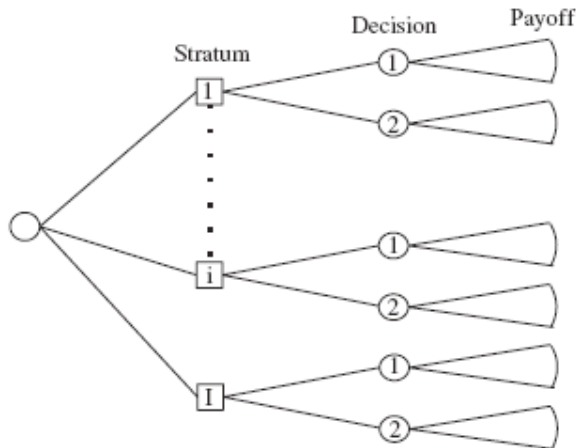
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Technical challenges in evaluating decision trees



Evaluating nested decision trees

- ▶ Alternation of *decision nodes* and *uncertainty nodes*
- ▶ Evaluating a tree of decision nodes (e.g., a traffic route): maximize at each step
- ▶ Evaluating a tree of uncertainty nodes (e.g., a casino game): simulate random draw at each step
- ▶ Evaluating an alternating tree: difficult!

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- ▶ Comparative decisions
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Decentralized decision making

- ▶ What is the role of the government/NGO?
- ▶ Coordinating data collection
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- ▶ Hierarchical modeling for dispersed decision making

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Advances in logistic regression

- ▶ Bayesian inference: the best fit to data does not give the best prediction for future data
- ▶ Conservatism in statistical inference
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Separation in logistic regression

```
glm (vote ~ female + black + income, family=binomial(link="logit"))
```

1960

	coef.est	coef.se
(Intercept)	-0.14	0.23
female	0.24	0.14
black	-1.03	0.36
income	0.03	0.06

1968

	coef.est	coef.se
(Intercept)	0.47	0.24
female	-0.01	0.15
black	-3.64	0.59
income	-0.03	0.07

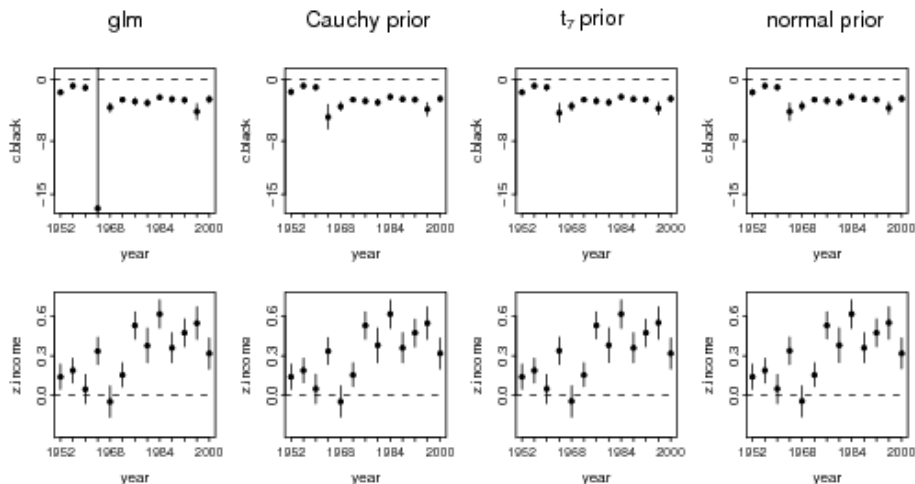
1964

	coef.est	coef.se
(Intercept)	-1.15	0.22
female	-0.09	0.14
black	-16.83	420.40
income	0.19	0.06

1972

	coef.est	coef.se
(Intercept)	0.67	0.18
female	-0.25	0.12
black	-2.63	0.27
income	0.09	0.05

Regularization in action!



Weakly informative priors for logistic regression coefficients

- ▶ Separation in logistic regression
- ▶ Some prior info: logistic regression coefs are almost always between -5 and 5 :
 - ▶ -5 on the logit scale takes you from 0.03 to 0.98
 - ▶ 5 on the logit scale takes you from 0.98 to 0.03
 - ▶ Smoking and lung cancer
- ▶ Independent Cauchy prior dists with center 0 and scale 2.5
- ▶ Rescale each predictor to have mean 0 and sd $\frac{1}{2}$
- ▶ Fast implementation using EM; easy adaptation of `glm`

Weakly informative priors for logistic regression coefficients

- ▶ Separation in logistic regression
- ▶ Some prior info: logistic regression coefs are almost always between -5 and 5 :
 - ▶ 5 on the logit scale takes you from 0.01 to 0.50 or from 0.50 to 0.99
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Evaluation using a corpus of datasets

- ▶ Compare classical glm to Bayesian estimates using various prior distributions
- ▶ Evaluate using cross-validation and average predictive error
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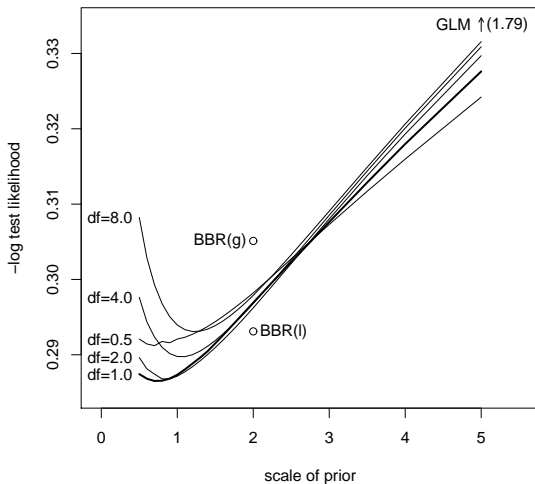
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Expected predictive loss, avg over a corpus of datasets



Conservatism of Bayesian inference

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- ▶ Problems with maximum likelihood when data show separation:
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