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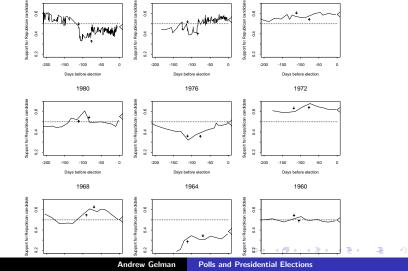
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1992

1984

Republican share of two-party preference in pre-election polls 1988



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- ▶ 2 months before election: candidates have been chosen, final campaign still to go
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- Fit model using elections since 1948, use to predict current election
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- Even during each Democratic and Republican conventions, all groups move in the same direction ("uniform swing")
- Consider a voter polled before the Republican convention

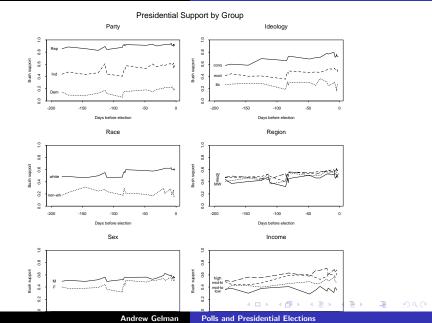
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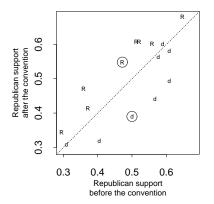
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Changes in Presidential campaign polls during Democratic and Republican conventions, 1964-1992

(conventions in 1988 circled)



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 Fit model to a series of polls before the 2000 election

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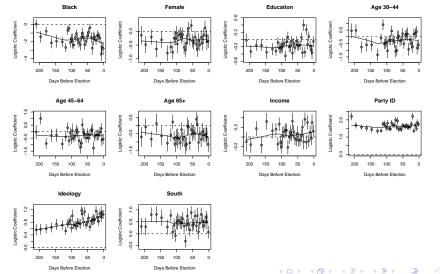
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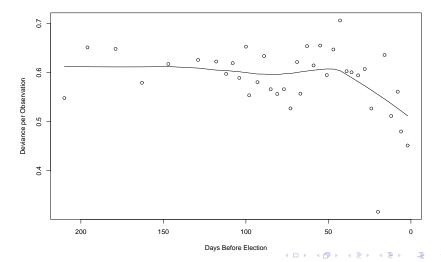
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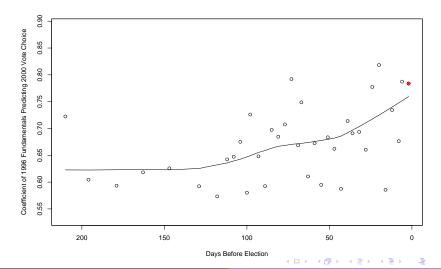
Increasing coefficients for fundamental predictors



Decreasing residual error of model of individual vote



Increasing predictive power for new data



The random-walk and mean-reversion models

- ► Random-walk model: voters are bounced around by campaign events, then the election comes
- ► *Mean-reversion model*: voters will mostly end up where predicted. It just takes them awhile to get there
- ► Mean-reversion model fits the data better, also explains why polls vary so much when elections are so predictable

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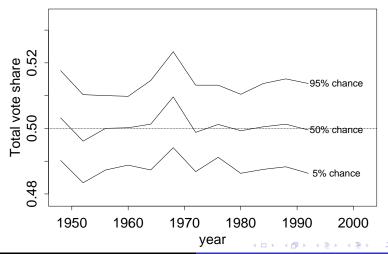
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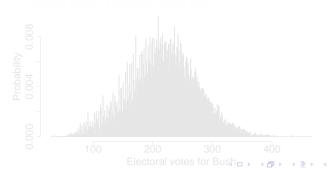
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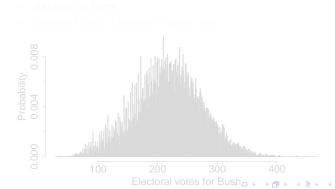
Percentage of the popular vote required for Democrats to have a given chance of winning the Electoral College



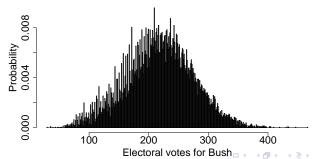
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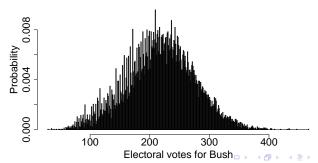
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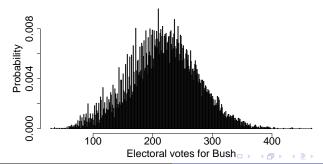
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- ► A state with N voters and E electoral votes

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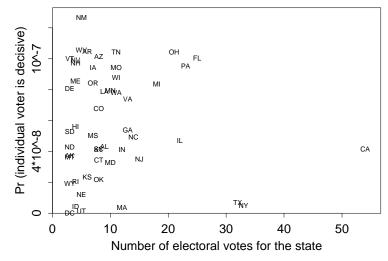
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- lacktriangle We said Pr(your state is tied) $\propto 1/N$
- ▶ Simple "binomial model" of random votes
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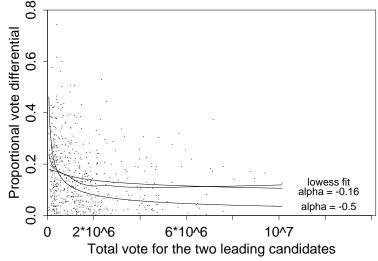
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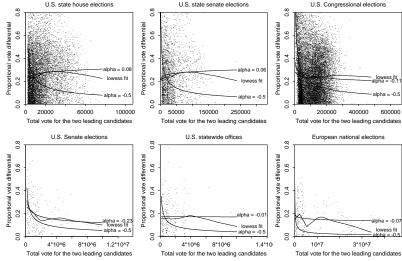
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Historical Pres. elections by state: vote margins vs. N



Other electoral systems: vote margins vs. N



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Rationality and voting: our explanation

- ▶ (Utility calculation: $\Delta U = pB c$)
- $\triangleright B = B_{\rm self} + \alpha N B_{\rm soc}$
 - B_{self} = individual benefit of your candidate winning
 B_{soc} = your view of the average social benefit of your candidate winning
 - a < 1 implying that you care less about other people to yourself
 - lpha>0 implying that you are not completely selfish
- Now B is proportional to N, and so it can be rational to act so as to improve your candidate's chance of winning
- Feedback keeps voter turnout stable: if turnout declines, then p increases, and it becomes more compelling to vote

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- ► The Electoral College favors voters in small states (so does the U.S. Senate!)
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- ▶ Pr(your vote is decisive) $\approx 10^{-7}$
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